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A flow-induced phase inversion in immiscible polymer blends containing a liquid-crystalline polymer studied by *in situ* optical microscopy

Marianne Astruc and Patrick Navard^{a)}

*Ecole des Mines de Paris, Centre de Mise en Forme des Matériaux,
UMR CNRS 7635, BP 207, 06904 Sophia Antipolis Cedex, France*

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Synopsis

The phase inversion from a morphology of hydroxypropylcellulose in water (HPC50%) droplets in polydimethylsiloxane (PDMS) matrix to a morphology of PDMS droplets in HPC50% matrix can be induced by a change of shear rate, due to a viscosity ratio inversion. Such a process passing through four different transient morphological stages was studied by optical microscopy in a transparent shear device. In a certain concentration region, at a fixed shear rate, after sheets of PDMS were formed, the transition “hesitates” between phase inversion and refined starting morphology. The influence of PDMS concentration, shear rate, elasticity, and phase dimension on the final morphology was investigated and compared with different models given in the literature. The influence of concentration and shear rate on the duration of the transient flow was also studied. We propose a simplified model of breakage of filament to explain a part of our results. © 2000 The Society of Rheology. [S0148-6055(00)01504-2]

I. INTRODUCTION

The increasing application of polymer blends for the elaboration of new materials is motivating the general interest in the study of morphology development in immiscible polymer blends, since morphology is one of the major factors controlling their final properties. For two-phase immiscible polymer blends, different morphologies such as droplet, fibrilla or co-continuous structures can be found. Several parameters are important in determining the final or steady-state morphology: composition of the blend, shear rate, viscosity and elasticity of the two phases, interfacial tension, and time of mixing. Among the many morphological phenomena that occur during preparation and processing of polymer blends, the study and prediction of the point of phase inversion at which co-continuity is observed has attracted a lot of attention. All the published studies are based on semiempirical models.

Some authors have related the point of phase inversion with the rheological properties of the components. Avgeropoulos *et al.* (1976) suggested that the point of co-continuity is reached when the torque ratio of the components in an internal mixer is equal to the component volume fraction ratio. Later, Paul and Barlow (1980) proposed a similar formulation using the viscosity ratio instead of the torque ratio. Miles and Zurek (1988) proposed the following generalized expression:

$$\frac{\Phi_A \eta_B(\dot{\gamma})}{\Phi_B \eta_A(\dot{\gamma})} \begin{cases} > 1: \text{phase } A \text{ is continuous} \\ = 1: \text{co-continuity} \\ < 1: \text{phase } B \text{ is continuous} \end{cases}, \quad (1)$$

where Φ_A and Φ_B are the volume fractions of the phases A and B , and η_A and η_B their viscosities at the applied shear rate $\dot{\gamma}$.

Several other models predicting the point of phase inversion are based on the filament instability concept. Metelkin and Blekht (1984) considered the dispersed phase to be that with the shorter breakage time of filaments. The critical volume fraction for the phase inversion was calculated to be

$$\Phi_B = \frac{1}{1 + \lambda F(\lambda)} \quad (2)$$

where

$$F(\lambda) = 1 + 2.25 \log \lambda + 1.81 (\log \lambda)^2, \quad (3)$$

with λ being the viscosity ratio of the blend components at the blending shear rate. Luciani *et al.* (1993) made the assumption that there is a two-fibrilla network structure at the co-continuity point. They supposed that the threads have the same length and stability at the phase inversion point, so that

$$\left(\frac{\Phi_B}{\Phi_A} \right)^{0.5} = \frac{\eta_A \Omega \left(\frac{\eta_B}{\eta_A} \right)}{\eta_B \Omega \left(\frac{\eta_A}{\eta_B} \right)} \quad (4)$$

where $\Omega(\lambda)$ is a function tabulated by Chappellear (1964).

Utracki (1991) suggested a model that can be used to predict the point of phase inversion for blends with a viscosity ratio far from unity. It is based on the dependence of the viscosity on the volume fraction of monodispersed hard spheres in the matrix, as proposed by Krieger and Dougherty (1959). The point of co-continuity is where the viscosity of polymer A (at the volume fraction Φ_A) dispersed in polymer B equals the viscosity of polymer B (at the volume fraction Φ_B) in polymer A . At this point, the ratio is

$$\lambda = \left[\frac{(\Phi_m - \Phi_B)}{(\Phi_m - \Phi_A)} \right]^{[\eta] \Phi_m}, \quad (5)$$

where $[\eta]$ is an intrinsic viscosity and $\Phi_m = 1 - \Phi_c$ is the maximum packing volume fraction. Φ_c is the critical volume fraction for percolation, equal to 0.156 for three-dimensional spherical dispersions [Chapoy (1986)]. An arbitrary value of $[\eta] = 1.9$ was given by Utracki (1991), based on published data on the points of phase inversion of thermoplastics and rubbers.

The model of Avgeropoulos predicts satisfactorily the point of phase inversion for torque ratios close to unity. The model of Miles and Zurek (1) and the model of Metelkin and Blekht (2) were found to overestimate the composition at which phase inversion occurs if the viscosity ratio departs from unity while the model of Utracki (5) was found to agree with some experimental results for blends having a viscosity ratio far from unity [Utracki (1991), Mekhilef and Verhoogt (1996), Mekhilef and Verhoogt (1997)]. The

agreement of these models with experiments is strongly dependent on the nature of the blend under consideration, underlining the imperfection of these models. The failure of the models may be due to the fact that the elasticity of each component polymer or the duration of the blending process are not taken into account. More recently, other models where the elasticity or the interfacial tension are considered have been established. Because the more elastic phase will tend to encapsulate the less elastic one and form the matrix, Bourry and Favis (1998) proposed the following expression for the point of co-continuity:

$$\frac{\Phi_A}{\Phi_B} = \frac{G'_B}{G'_A} \cdot \frac{G''_A}{G''_B}, \quad (6)$$

where G'_i and G''_i are, respectively, the storage and the loss modulus of the component i . This expression seems to give better results than expressions (1), (2), and (5) when the elasticities of the two components differ strongly. By considering a co-continuous structure as a dense packing of randomly oriented rodlike particles of the minor phase and taking into account the microrheological requirements for the stability of such rods, Willemse *et al.* (1998) established an equation predicting the range of compositions within which fully co-continuous structures can exist. The equation relates the critical volume fraction of the minor phase at complete co-continuity $\Phi_{d,cc}$ to the matrix viscosity η_m , interfacial tension σ , shear rate $\dot{\gamma}$ and phase dimension R_0 :

$$\frac{1}{\Phi_{d,cc}} = 1.38 + 0.0213 \left(\frac{\eta_m \dot{\gamma}}{\sigma} R_0 \right)^{4.2}. \quad (7)$$

An absolute prediction based on this model is not straightforward because the phase dimension has to be measured (or even worse, has to be defined for a real blend). The authors have experimentally shown that $\Phi_{d,cc}$ is slightly influenced by η_m [Willemse *et al.* (1998)] whereas an increase of σ leads to an increase of $\Phi_{d,cc}$ and a decrease of the range of co-continuity [Willemse *et al.* (1999a)].

Flow-induced phase inversion occurs when the original morphology of polymer A dispersed in the matrix of polymer B is transformed under the action of a flow into polymer B dispersed in polymer A. Clearly, this must involve crossing the point of co-continuity. Such crossings have been observed after blend extrusion [Shih (1992)] and studied in batch mixers [Shih (1995), Ratnagiri and Scott (1996)]. In some cases, the observations could be explained by differences in the melting temperature of the components (i.e., phase A supposed to be the matrix is molten at a higher temperature than phase B, which gives solid A in molten B, and which inverts when A melts). But it appears clearly that in most cases, a variation of viscosity or elasticity during the blending process plays a major role [Ratnagiri and Scott (1996), Ratnagiri and Scott (1997)]. The main problem is that observations after extractions do not allow us to clearly know how co-continuity is reached during the flow and how the morphologies change around that point. This lack of knowledge makes it difficult to build a comprehensive model. To our knowledge, no *in situ* experiment on this effect has been reported.

Using the torque or viscosity ratio concept, one may understand qualitatively how a phase inversion can be induced by the flow. By varying the shear rate, the viscosity ratio may vary. If this variation is large enough, it could induce a phase inversion [Eqs. (1), (4) or (5), depending on the model]. Bouilloux *et al.* (1997) studied a phase inversion induced by the variation of viscosity ratio with time of mixing. By quenching the blend at various stages of mixing, they always observed the co-continuous structure. They could not reach the inverted morphology. Willemse *et al.* (1999a) assumed that sheets of the

initial dispersed phase could be the precursors of the co-continuous morphology. Depending on the stability of the network of ligaments in the mixer after sheet breakup, the co-continuous morphology could be either a transient or a stable morphology. The formation and the stability of these kinds of sheets under a simple shear flow in viscoelastic blends was first reported by Sundararaj *et al.* (1995). More recently, Lazo and Scott (1999) confirmed with extraction experiments on PS/PE blends that phase inversion in steady-shear flow pass through sheet formation. Sheet formation that transforms into threads or drops seems to be an important factor in polymer blend deformation [Willemse *et al.* (1999b)].

The objectives of the present work are to use rheo-optical tools to visualize a shear-induced phase inversion in an immiscible polymer blend, to study how it occurs, and to compare this to the theories that are available. For reasons that will be detailed later, we used a blend of PDMS and a solution of hydroxypropylcellulose in water (HPC50%). One of the difficulties in studying phase inversion and how it occurs is that the point of phase inversion is classically reached by increasing concentration, which implies changing samples. The advantage of the phase inversion observed here is that the co-continuous morphology should be a transient state that takes place between two droplet-matrix morphologies, in the same sample. This opens the way to study two related phenomena, i.e., the mechanisms controlling both the co-continuity and the phase inversion.

II. EXPERIMENTAL SETUP AND PREPARATION PROCEDURES

A. Rheo-optical tools

Flow-induced morphology observations were performed on a rheo-optical system comprising three main parts:

- (i) A Linkam CSS 450 shearing system. It is composed of two transparent rotating parallel plates permitting the observation of the sample at 7.5 mm from the center axis of rotation. The shearing system is monitored by a PC using the LINKSYS 1.41 software.
- (ii) An optical system composed of an optical microscope Leitz Metallux 3 with a lighting system, a charge-coupled device camera, and a monitor.
- (iii) A video data acquisition system (video recorder and time code generator).

1. Experimental difficulties

From a practical point of view, the study of phase inversion mechanisms with rheo-optical tools is not simple. The formation of co-continuous structures in polymer blends requires a relatively high concentration of both components. But the observation of morphology in concentrated blends is difficult: concentrated blends are highly scattering and so turbidity limits observation of their morphology by optical microscopy. That is why it was chosen to shear thin layers (a gap between 50 and 100 μm). We are aware of the fact that this restriction could influence the morphologies. But this is the only way to perform *in situ* observations with such highly concentrated systems. In the experiments special care was taken to ensure that the observations are not significantly modified by the small dimensions of the gap.

Furthermore, due to the complex morphologies that were formed, it is difficult to identify each phase and to recognize which polymer is where. A way to overcome this is to label one of the polymers. By choosing an isotropic component and a birefringent one, it is possible to distinguish the two phases between crossed polarizers. Unfortunately, our

blends are liquid at room temperature and do not allow us to carry out extraction experiments after the shear experiments.

B. Selected materials

Materials with the required rheological and optical properties were selected. All experiments were performed on blends of PDMS from Rhône-Poulenc (Rhodorsil 47V200000, $M_w = 149\,350$) and a solution of hydroxypropylcellulose diluted by 50 wt% in water (HPC50%). The HPC is produced by Aqualon (Klucel L, $M_w = 100\,000$). These components are liquid at room temperature. To avoid problems of phase separation that have been reported for the solution of 50% of HPC in water [Guido and Grizzuti (1995)], the experiments were performed at 18 °C. Under these conditions, the solution of HPC is in a liquid-crystalline phase. It is birefringent, whereas the PDMS is not. It is thus possible to distinguish the two components by using depolarized light microscopy. We take a literature value of the interfacial tension equal to 12.2 mN/m as reported by Tsakalos [Tsakalos (1995)] as obtained for 50 wt% HPC (Klucel L) in a PDMS (Rhodorsil) matrix.

1. Rheology

The steady shear viscosity measurements of the pure components were carried out at 18 °C with a controlled stress Stresstech Rheologica rheometer, in parallel plate geometry (1 mm gap and 25 mm diameter). Shear rates from 0.1 to 20 s⁻¹ were investigated. The measurements performed on the HPC solution were made after sufficient large deformations to reach the steady-state conditions in lyotropic LCPs [Moldenaers (1987)]. Viscosity data of the two components are presented in Fig. 1(a). The zero shear viscosity of the PDMS is 240 Pa s compared with 480 Pa s at 0.1 s⁻¹ for HPC50%. Below 8 s⁻¹, the PDMS is Newtonian while the HPC50% solution presents a strong shear thinning behavior. The viscosity curves cross at a shear rate of 0.8 s⁻¹. Below this shear rate, the PDMS is the least viscous component while above it is the most viscous. Over the shear rate range under investigation (0.1–20 s⁻¹), the viscosity ratio of the components can easily be changed by varying the shear rate. Different viscosity ratios depending on the shear rate are specified in Table I. By changing the shear rate from 0.2 to 10 s⁻¹, the viscosity ratio varies from 1.7 to 0.4.

First normal stress difference N_1 data are plotted in Fig. 1(b). Below 12 s⁻¹, the solution of HPC50% has the highest elasticity. This is confirmed by the measurements of the storage and loss moduli carried out at a stress of 100 Pa. At low frequencies, the solution of HPC50% has the highest elasticity while the loss modulus is the lowest (Fig. 2). The storage moduli cross at 11 rad s⁻¹ and the loss moduli at 0.30 rad s⁻¹, close to the values found in steady-state experiments. Even if the Cox–Merz rule is not strictly verified for the HPC solution, these results show that dynamics measurements allow us to compare the relative elasticity of both components, especially for the higher shear rates that cannot be reached in continuous measurements.

C. Preparation of the blends

Preparation of the solutions of HPC was made following the method described by Tsakalos (1995). To avoid possible diffusion of water in PDMS that could change the HPC concentration in the HPC50% component, the PDMS was saturated with water before blending [Tsakalos (1995)].

In order to study phase inversion induced by a change in the viscosity ratio, it was necessary to prepare blends for which the PDMS is the continuous phase at rest. During

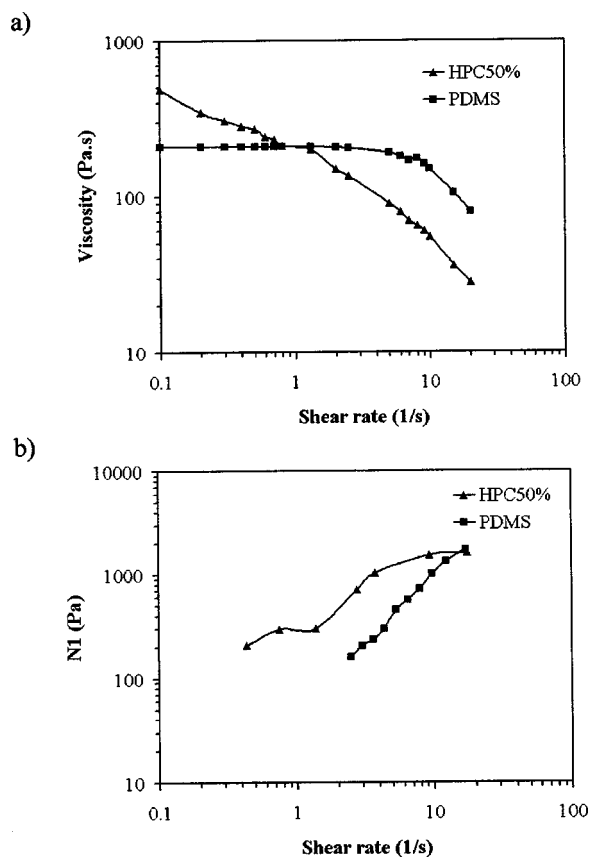


FIG. 1. Shear viscosity (a) and N_1 (b) of PDMS and HPC50% measured at 18 °C in a plate-plate geometry.

this blending procedure, special care was taken not to cross the point of phase inversion. This means that the samples had to be submitted to very low shear rates (under 2 s^{-1}). The blends were hand mixed after cooling in a refrigerator. Suitable amounts of the components were weighed and mixed very slowly for ~ 10 min with a spatula until a homogeneous creamy appearance was obtained.

For the preparation, two opposite points have to be balanced. On one side, the blends have to be mixed during sufficientl long time and with sufficientl high speed of rotation to give a good homogenization and stability. On the other hand, for high concentrations of the dispersed phase, the point of phase inversion is easily crossed under these conditions. A phase separation is observed after a few hours and it is also difficult to reproduce the same initial morphology for different samples with the same concentrations. Blends of 70, 67, 63, 60, and 55 vol. % of PDMS were prepared by this procedure. They are, respectively, referred to PDMS70, PDMS67, PDMS63, PDMS60, and PDMS55. We were not able to prepare blends with a lower concentration of PDMS where PDMS was the continuous phase at rest.

D. Experimental conditions

Startup experiments in the Linkam shearing system were carried out at different shear rates ($0.8\text{--}30 \text{ s}^{-1}$) and concentrations (55%–70% of PDMS). The indicated shear rates correspond to the shear rates applied at the location of observation in plane-plane ge-

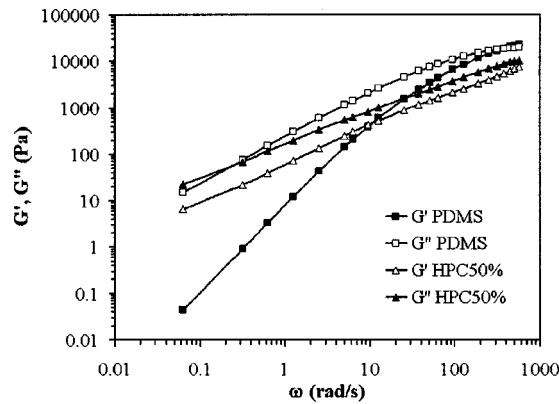
TABLE I. Viscosity ratio and storage modulus ratio of the HPC50% and the PDMS at 18 °C calculated at constant shear rate.

Shear rate (1/s)	$\eta_{\text{HPC50\%}} / \eta_{\text{PDMS}}$	$G'_{\text{HPC50\%}} / G'_{\text{PDMS}}$ ^a
1.5×10^{-3}	7.3	—
0.2	1.7	40
0.5	1.3	11
0.8	1	9.8
2.5	0.7	3.1
10	0.4	1
15	0.4	0.8
20	0.4	0.7
30	0.4 ^b	0.5

^aAssuming that the Cox–Merz rule is verified^bValue extrapolated from Fig. 1(a).

ometry, given the thickness of the sample and speed of rotation. All the experiments were done at $\pm 8\%$ of the indicated shear rates. These variations are associated with the radial gradient of the shear rate throughout the width of visualization. First, the transient flow for blends with concentration of PDMS varying from 55% to 70% was studied at a startup of 10 s^{-1} . Second, the transient flow of PDMS63 was studied under different startup experiments with shear rates varying from 0.8 to 30 s^{-1} . The lower limit of the range of concentrations is limited by the difficulties of preparation described in the preceding section (phase inversion may occur during the blending procedure). The highest value of shear rate that can be used is 30 s^{-1} , above which the blend is expelled from the shearing device after few minutes of shearing.

In Sec. III, the transient flow observed for the blends at a shear rate of 10 s^{-1} will be presented in detail. These results illustrate the typical mechanisms occurring during a well-controlled but highly specific flow induced phase inversion.

**FIG. 2.** Storage and loss modulus data of PDMS and HPC50% measured at 18 °C in a cone and plate geometry.

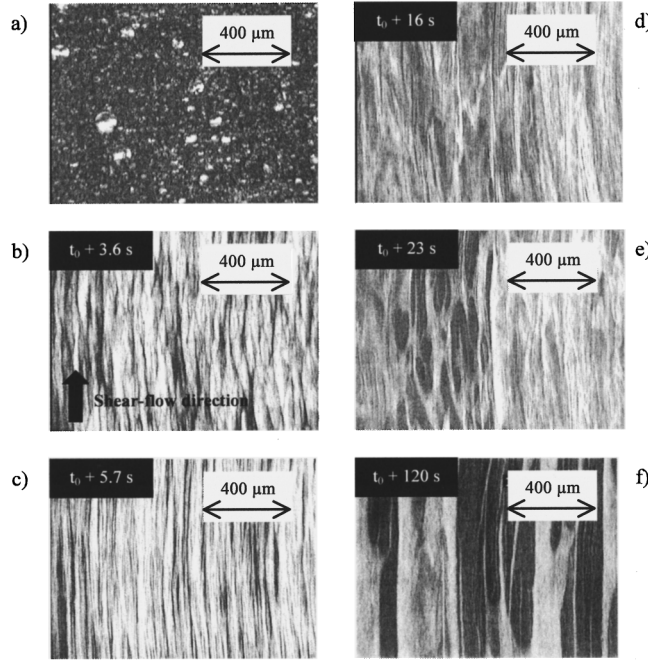


FIG. 3. The different morphologies of the blends PDMS/HPC50% observed between crossed polarizers in the Linkam device at 18 °C. The PDMS appears black and the HPC50% bright. (a) At-rest morphology of the blend PDMS60. (b) and (c) Morphology of the blend PDMS67 during the first stage of shearing at 10 s^{-1} . (d) and (e) Morphology of the blend PDMS60 and (f) the blend PDMS67 during the second stage of shearing at 10 s^{-1} .

III. RESULTS AND DISCUSSION

A. Observed morphologies

1. At-rest morphology

After carefully and slowly filling the Linkam shearing system with a small amount of blend and adjusting the gap, the sample was allowed to relax and to reach a temperature of 18 °C for 30 min. For the concentrations of PDMS from 55% to 70%, similar morphologies were observed [Fig. 3(a)]; droplets of HPC50% of diameter under $100 \text{ }\mu\text{m}$ are dispersed in the matrix of PDMS. Some droplets contain small subinclusions of PDMS. Favis and Chalifoux (1988) and Bourry and Favis (1998) reported the presence of similar encapsulations in blends of polypropylene/polycarbonate and in blends of polyethylene/polystyrene around the point of phase inversion. In our blends, we attribute the presence of these encapsulations in the at-rest morphology to the fact that some local phase inversion may have occurred during the blending preparation.

2. Transient morphologies (example of shear at 10 s^{-1})

Submitted to a simple shear flow at a shear rate of 10 s^{-1} , the blend is in a region where a phase inversion is expected to take place. Several different transient morphologies were observed before the final steady-state equilibrium morphology was reached. Four different stages in the mechanism leading to the final equilibrium can be distinguished. These four stages occurred in all the observed blends and can be considered as the general route that the PDMS/HPC50% blends take toward phase inversion.

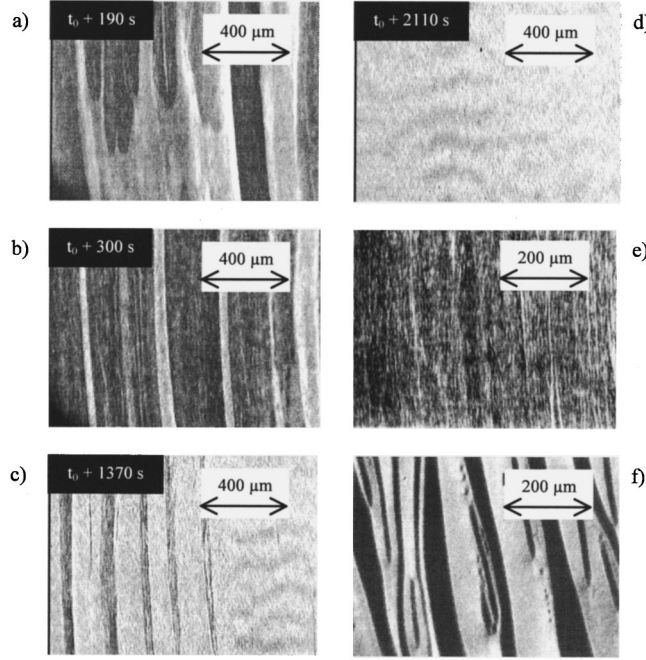


FIG. 4. In the blend PDMS60: (a) the large domains of PDMS are stretched along the flow direction; (b) stripes of continuous phases of PDMS and continuous phases of HPC50% are formed; (c) the stripes of PDMS become thinner. Filaments originating from these stripes are dispersed in the continuous phase of HPC50%; (d) The stripes of PDMS have completely disappeared and the phase inversion has propagated through the whole sample. We can observe a continuous phase of HPC50% with droplets of PDMS inside. This is case (b) of Fig. 5. (e) In PDMS67: at the end of the fourth stage, the stripes of local phase inversion have disappeared: the flow-induced phase inversion does not occur and the final morphology consists of droplets of HPC50% in the continuous phase of PDMS, as shearing. The difference is the much smaller size of the HPC50% droplets [see Fig. 3(a)]. This is case (c) of Fig. 5. (f) PDMS67 sheared 15 h at 0.2 s^{-1} after phase inversion.

First stage ($t_0 \rightarrow t_0 + 10 \text{ s}$ at 10 s^{-1}): bi-fibrilla morphology. During the first 10 s of shearing at 10 s^{-1} , the inclusions of HPC50% and the subinclusions of PDMS are deformed and stretched along the flow direction [Fig. 3(b)]. Soon after, it is difficult to tell which phase is the continuous one. The PDMS and the HPC50% phases appear like long filaments and the morphology can be described as a bifibrilla structure [Fig. 3(c)].

Second stage ($t_0 + 10 \text{ s} \rightarrow t_0 + 60 \text{ s}$ at 10 s^{-1}): emergence of sheets of PDMS. The bifibrilla morphology is not stable. The shorter filaments of PDMS begin to break [Fig. 3(d)] while at the same time, sheets of PDMS layered in the flow direction form [Fig. 3(e)]. These domains of PDMS contain filaments and droplets of HPC50% with small subinclusions of PDMS. They are dispersed in a continuous phase of HPC50% also containing small droplets stemming from the shorter filaments of PDMS [Fig. 3(f)].

Third stage ($t_0 + 60 \text{ s} \rightarrow t_0 + 600 \text{ s}$ at 10 s^{-1}): stripe morphology. For a longer shearing time, the sheets of PDMS continue to stretch along the flow direction [Fig. 4(a)] until they form stripes: continuous phases of HPC50% with small droplets of PDMS dispersed alternately with continuous phases of PDMS containing inclusions of HPC50% with subinclusions of PDMS [Fig. 4(b)]. In fact, we can consider that by this stage, a phase inversion has already occurred in the stripes of HPC50%, between the stripes of PDMS.

Fourth stage ($t_0 + 600 \text{ s} \rightarrow t_0 + 10\,000 \text{ s}$ at 10 s^{-1}): homogenization of the morpholo-

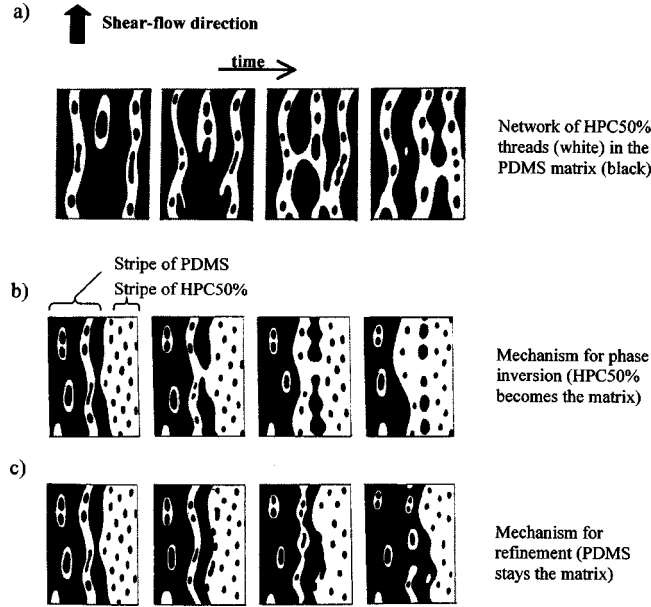


FIG. 5. (a) Schematic representation of the network of threads of HPC50% in the stripes where the PDMS is the continuous phase observed during the fourth stage. (b) Schematic representation of the mechanisms observed at the edge of the stripes during the fourth stage when a filament of HPC50% is close to the edge: the edge of PDMS breaks up and the stripe of HPC50% enlarges. (c) The filament of HPC50% breaks up and the stripe of HPC50% thins.

gy. After the stripes have been formed, the morphology evolves extremely slowly. Different mechanisms occur independently in different zones in the blend.

(i) In the stripes where the PDMS is the continuous phase, we observe long filament of HPC50% constituting a kind of relatively unstable network in which branches are continuously forming and breaking. Some of these filament break to form smaller droplets. These small inclusions coalesce to reform filaments. Inside the inclusions of HPC50%, the subinclusions of PDMS are also subject to the mechanisms of breakup and coalescence. As the inclusions of HPC50% form filaments we also observe small droplets of PDMS coalescing to form filaments. In droplets of HPC50%, one or two encapsulated drops of PDMS can generally be observed. These mechanisms are shown schematically in Fig. 5(a).

(ii) In the stripes where the HPC50% is continuous, filament and inclusions of PDMS break to form small droplets. Although it is not easy to measure it by optical microscopy, their size distribution seems to be very narrow compared with the size distribution of the inclusions of HPC50% in the stripes of PDMS. This could be due to an absence of coalescence of PDMS droplets in these stripes.

(iii) At the boundary between PDMS and HPC50% stripes, several complex mechanisms compete.

Droplets of PDMS dispersed in the matrix of HPC50% can coalesce with the stripes of PDMS and contribute, in this way, to the broadening of the PDMS stripes.

The existence of a filament of HPC50% at the edge of a stripe of PDMS can lead to two opposite mechanisms.

The layer of PDMS between the filament of HPC50% and the stripe of HPC50% can also constitute a filament. Depending on the breakage time of this filament (whether it is

shorter or longer than that of HPC50%), the stripe of PDMS will be broader or become thinner. In the case of the development of Rayleigh instabilities in the thread of PDMS, the drops created will disperse in the stripe of HPC50%. The filament of HPC50% joins the continuous phase of HPC50% and the subinclusions of PDMS encapsulated in this filament are thus dispersed in the stripe of HPC50% too. *This mechanism leads to the broadening of the stripes of HPC50% and so to the phase inversion.* It is schematized in Fig. 5(b). If the breakage time of the filament of HPC50% is shorter than that of the filament formed by the layer of PDMS, most of the droplets of HPC50% created will contain subinclusions of PDMS. *This mechanism leads to the broadening of the stripes of PDMS and to the refinement of the initial morphology.* This mechanism is schematized in Fig. 5(c).

After such long shearing times, two different equilibrium morphologies can thus be obtained. In some cases, due to the thinning of the stripes of PDMS, the local phase inversion propagates into the whole sample [Figs. 4(c) and 4(d)]. Consequently, a general flow-induced phase inversion occurs. In other cases, the stripes of HPC50% thin and disappear. The flow-induced phase inversion does not take place. As can be seen in Fig. 4(e), the resulting final morphology is in this case a continuous phase of PDMS with filament and droplets of HPC50% that themselves contain subinclusions of PDMS.

We did not note any influence of the radial gradient of the shear rate over the width of visualization during these experiments. Indeed the formation and the broadening of the different stripes did not occur preferentially at one side of the window.

Some experiments were performed at higher gaps (up to 500 μm) to check the weak influence of the gap. We observed with less sharpness the morphologies of the blends but their evolution was similar as for small gaps (50 or 100 μm). This was confirmed once the shear was stopped at different stages, and the gap was slowly decreased up to the point where it was possible to observe the morphology distinctly. This is not direct *in situ* experiments, but interrupted ones.

3. Evolution of the final morphology after cessation of flow

Once the final morphology was reached, the shear was stopped. For the blends where the phase inversion did not occur, a morphology similar to the initial morphology before shearing, but much finer, develops a few minutes after cessation of flow. The PDMS is the continuous phase, and the dispersed phase is composed of droplets of HPC50% that encapsulate between one and three droplets of PDMS. This morphology is similar to the morphology of high-impact polystyrene.

If the flow is stopped after a phase inversion, a completely opposite morphology is observed. Immediately after stopping, the shear-deformed droplets of PDMS relax into spherical drops. The drops of PDMS coalesce but remain in the dispersed phase. In order to confirm the stability of the inverted morphology (blends with HPC50% continuous and PDMS dispersed) and the nonreversibility of the phase inversion, these blends were resheared 2 min after cessation of flow at 0.2 s^{-1} , a shear rate where PDMS should be the continuous phase. But even after 15 h of shear, the HPC50% was still the continuous phase as shown in Fig. 4(f).

B. Influence of polymer concentration and shear rate on the final steady-state morphology

At 10 s^{-1} , whether a phase inversion is induced or not depends on concentration. As shown in Fig. 6, the occurrence of phase inversions observed during the tests at a given concentration increases with the concentration of HPC50%. With 60% of PDMS, the

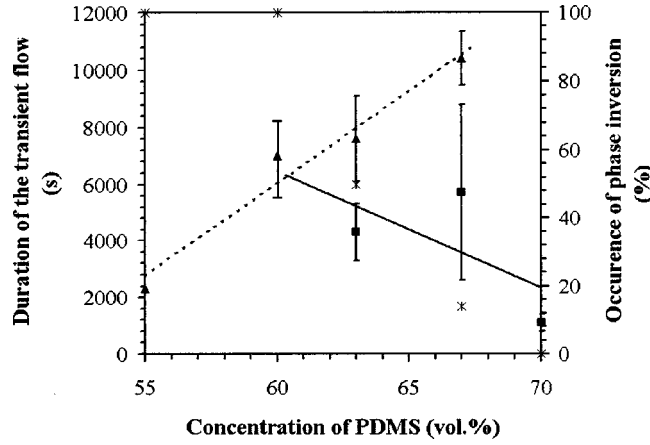


FIG. 6. Blends sheared at 10 s^{-1} . Occurrence of phase inversion (*) vs concentration of PDMS. Duration of the transient flow t_3 vs concentration of PDMS in case of phase inversion (▲) and refinement (■). The lines (---) and (—) are linear fit of the experimental points.

phase inversion is always observed. With 70% of PDMS, a phase inversion is never induced. Between these two limits, there is a range of concentrations where, for the same blend, we obtain in some cases the inverted morphology after shearing and in other cases not. The HPC50% viscosity being very sensitive to temperature, small variations could modify the viscosity ratio. Furthermore because the initial morphologies are not well controlled for the reasons discussed above, small differences in the at-rest morphologies (size of the inclusions, volume of PDMS encapsulated or small variations of concentrations) could influence the final morphology after shearing at 10 s^{-1} near the region of phase inversion. All these parameter variations could be sufficient to shift the system into or out of the region of phase inversion.

As co-continuity was observed for a range of concentrations instead of a single point of phase inversion, the critical concentration for flow-induced phase inversion cannot be determined by one point. There is rather a range of concentration for the blend to “hesitate” between both morphologies. Nevertheless, without extraction experiments we cannot confirm that the final steady-state morphology is passing through a transient co-continuous morphology.

1. Comparison with models based on viscosity ratio and elasticity ratio

Our observations can be compared with the different models presented in the literature. From Eqs. (1), (2), and (5), the viscosity ratio necessary to have HPC50% as the continuous phase can be calculated for each concentration. The minimal shear rate to apply for having a continuous phase of HPC50% can be inferred from the rheological data in steady state [see Fig. 1(a)]. But since in the absence of interfacial slip the stresses are continuous across the interface while the deformation rates are not, the models have in common the fact that they consider only the viscosity ratio should be used at constant stress as reported by Utracki (1991). Calculations based on constant stress of one of the two phases give similar results as made at constant shear rate for the models of Miles and Zurek [Eq. (1)] and Metelkin and Blekht [Eq. (2)] (see Table II). Data calculated with the model of Utracki [Eq. (5)] depend on the way the viscosity ratio is calculated and cannot be compared with our experimental results. In the case of Bourry and Favis [Eq. (6)], the

TABLE II. Minimal shear rate to apply to have HPC50% as the continuous phase determined with the models of Miles and Zurek [Eq. (1)], Metelkin and Blekht [Eq. (2)], Utracki [Eq. (5)], and Willemse *et al.* [Eq. (7)] for blends of different concentrations [(i) calculated at constant shear rate; (ii) calculated at constant shear stress of HPC50%; (iii) calculated at constant shear stress of PDMS].

Blend	Shear rate (s^{-1}) calculated with the different equations			
	[Eq. (1)]	[Eq. (2)]	[Eq. (5)]	[Eq. (7)] ^a
PDMS55				
(i)	1.8	1.7	3.1	
(ii)	1.8	1.7	2.9	7.5
(iii)	1.5	1.2	1.8	
PDMS60				
(i)	2.2	1.7	7	
(ii)	2.2	1.7	5.5	7.8
(iii)	1.6	1.2	2.1	
PDMS63				
(i)	3.1	1.7	No	
(ii)	2.9	1.7	9	8.5
(iii)	1.8	1.2	2.5	
PDMS67				
(i)	4.6	1.8	No	
(ii)	4	1.8	13	10
(iii)	2	1.5	2.8	
PDMS70				
(i)	7	1.8	No	
(ii)	5.5	1.8	30	14
(iii)	2.1	1.5	31	

^aFitted at $10 s^{-1}$ with our experimental results, using $R_0 = 23 \mu m$.

necessity to know G' and G'' at constant shear stress (that we did not measure) does not allow us to perform such a comparison.

At $10 s^{-1}$, PDMS and HPC50% have about the same elasticity (see Table I), which strongly simplifies evaluation of the influence of viscosity and elasticity on the point of phase inversion. Nevertheless, the models of Miles and Zurek [Eq. (1)] and Metelkin and Blekht [Eq. (2)] have limits. For shear rates above $7 s^{-1}$, they predict a phase inversion on all of our blends. However, refinement is observed for some blends with 63% of PDMS or more.

For shear rates below unity, the elasticity ratio and viscosity ratio are greater than unity. They should have opposite effects on the morphology. In order to test the influence of elasticity on the final morphology, a blend of PDMS63 was sheared at $0.8 s^{-1}$ (viscosity ratio = 1) for 30 h (i.e., 86 400 strain units). After a few hours, the stripe morphology appeared and no more evolution of the morphology was observed during the following 20 h of shearing. We did not get a phase inversion, as predicted by Eqs. (1) and (2) that nevertheless do not take into account the elasticity ratio.

Between 10 and $30 s^{-1}$, the elasticity ratio changes with the shear rate (from 1 to 0.5) while the viscosity ratio remains at a constant value of 0.4. By increasing the shear rate and so decreasing the elasticity ratio, elasticity should limit the phase inversion. On the contrary, we observed with PDMS63 blends either phase inversion or refinement with even a slight increase of the rate of occurrence of phase inversion (Fig. 7).

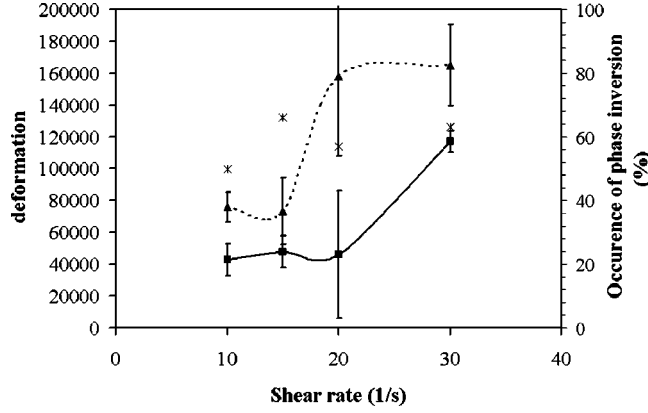


FIG. 7. Deformation in strain units necessary to reach either the refine (—■—) or the phase inverted morphology (---▲---) and frequency of occurrence (*) of phase inversion vs shear rate for the blend PDMS63.

The elasticity ratio does not seem to influence the concentration of shear-induced phase inversion for elasticity ratios between 0.5 and 10. But we have clear experimental limitations for exploring higher elasticity differences.

2. Comparison with the model of Willemse *et al.*

Although the model of Willemse *et al.* [Eq. (7)] presents the disadvantage of having the phase dimension as an unknown parameter, it has the advantage of taking into account more mixing parameters such as viscosity of the major phase, shear rate, and interfacial tension, which are well defined in our experiments. Contrary to the other models, this model does not allow us to predict a point of phase inversion but a minimal concentration so that the initial dispersed phase becomes a continuous phase. Equation (7) was used to predict the effects of concentration or shear rate by using the phase dimension R_0 as a fit parameter.

At 10 s^{-1} , the minimal concentration to have HPC50% as a continuous phase is experimentally known: phase inversion is observed with a minimal concentration of HPC50% of 33% (blend PDMS67). Knowing the shear rate, concentration of HPC50% ($\Phi_{\text{HPC50\%,cc}}$), matrix viscosity and interfacial tension R_0 can be calculated with Eq. (7). This is justified because the phase dimension R_0 only changes during the initial stage of mixing. By supposing that the phase dimension is slightly influenced by concentration in this concentration range, the critical shear rates for phase inversion can be calculated for the different concentrations. The results are presented in Table II (with $R_{0\text{HPC50\%}} = 23 \mu\text{m}$ for PDMS67).

Ghodgaonkar and Sundararaj (1996) proposed a formulation to predict D , the dispersed phase drop diameter in viscoelastic blends

$$D = \frac{2\sigma}{\eta_m \dot{\gamma} - 2(G'_d - G'_m)}, \quad (8)$$

with G'_d and G'_m the storage moduli of the dispersed and matrix phases. If we calculate D with HPC50% as the dispersed phase and PDMS as the matrix, we do not find major differences in the range of shear rates calculated with Eq. (7) (see Fig. 8). This can justify the use of a constant phase dimension R_0 in Table II. Because of the qualitative deter-

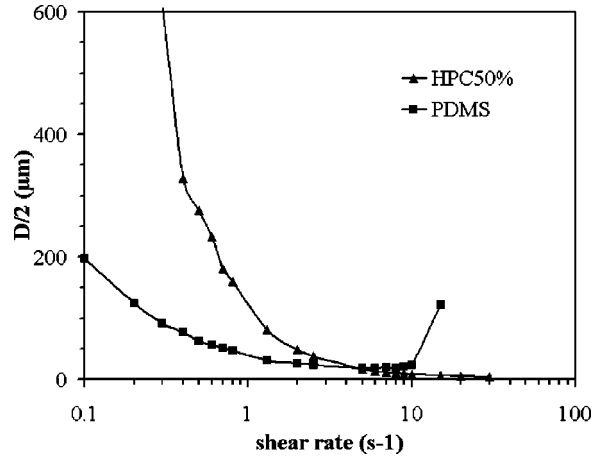


FIG. 8. Radius of the dispersed phase versus shear rate calculated with Eq. (8) proposed by Ghodgaonkar and Sundararaj (1996).

mination of $\Phi_{\text{HPC50\%,cc}}$ and R_0 , these results do not allow us to determine quantitative values but to highlight a trend: the minimal shear rate to apply for having HPC50% as the continuous phase increases with concentration of PDMS.

By reversing the role of PDMS and HPC50% in Eq. (7), the apparent stability of the inverted morphology (blends with HPC50% continuous and PDMS dispersed) and the nonreversibility of the phase inversion at low shear rates can be understood. We calculated at 0.2, 0.8, and 10 s^{-1} the minimal phase dimension R_0 of PDMS necessary to return as the continuous phase. With 67% of PDMS, R_0 of PDMS should be larger than 263 μm at 0.2 s^{-1} , 108 μm at 0.8 s^{-1} , and 46 μm at 10 s^{-1} to return as the continuous phase. This is much larger than what is experimentally observed at 0.2 s^{-1} [Fig. 4(f)] and 10 s^{-1} [Fig. 4(d)] or calculated with Eq. (8) (see Fig. 8).

C. Phase change dynamics: Time necessary to reach the steady-state morphology

The existing models give no information about the duration of the flow before the occurrence of phase inversion. Lazo and Scott (1999) made the assumption that the relevant parameter in the kinetics of phase inversion of PS/PE blends is the rate of hole nucleation in the forming sheets. But the sheets are formed with the least viscous component. They are so more easily stretched than if they were formed with the most viscous component. Phase inversion occurs after 1000–3500 strain units. In our case, the sheets of PDMS seem to be more stable. Our observations have shown that the time necessary to reach the inverted morphology is very long. The mechanisms leading to the final steady-state morphology seem to occur at the edge of the sheets and not on their whole surface as proposed by this hole nucleation theory. Furthermore, it does not explain the case of refinement. This mechanism is certainly present but not prevalent in our blends.

We can attribute a characteristic time to the different identified transient stages of the flow. For each type of blend, measurements were carried out for at least four or five samples. We define t_0 as the start of shearing, t_1 as the time when the large domains of PDMS emerge (equivalent to the beginning of the second stage of morphology as described in the preceding paragraph), t_2 as the beginning of the stripe morphology (equivalent to the beginning of the fourth stage of morphology) and t_3 as the time

TABLE III. Characteristic times of the three identified steps to reach the final steady-state morphology, for blends of different concentrations sheared at 10 s^{-1} .

Final steady-state morphology	Blend	t_1 (s)	t_2 (s)	t_3 (s)	$\dot{\gamma}t_3$ (strain units)
Phase inversion	PDMS60	23	310	7000	70 000
	PDMS63	47	160	7600	76 000
	PDMS67	60	260	10 400	104 000
Refinement	PDMS63	54	180	4300	43 000
	PDMS67	330	910	5700	57 000
	PDMS70	23	61	1100	11 000

necessary to reach the steady-state morphology (equivalent to the end of the fourth state of morphology). The boundary between the different stages is not very sharp, especially between the second and third stage. Actually, formation of the large domains of PDMS can continue while others are already being stretched to form stripes. Furthermore, it is difficult to determine the end of the last stage for the blends for which the inverted morphology does not occur. By contrast, for the blends that invert their morphology, we can easily determine the time t_3 when the last filament of PDMS breaks up in the matrix of HPC50%. The results are given in Tables III and IV. It is clear that most of the time necessary to reach the steady-state morphology (refinement or phase inversion) is devoted to the t_3 process. Compared to t_2 and t_3 , the time necessary to obtain the bifibrillar morphology is very short, being nevertheless a few hundred strain units. The time t_2 necessary for obtaining the stripe morphology is much larger, and the corresponding deformation is a few thousands strain units. The limiting process is the interplay between coalescence and breakup that occurs during the fourth stage. It is also during this stage that the system will either refine its morphology or phase invert. The description of the phase inversion must thus take into account this stage. The other stages can be ignored as a first approximation. We will now go into more details on the influence of concentration and shear rate on the transition to the final morphology.

TABLE IV. Characteristic times and deformation necessary to reach the steady-state morphology at different shear rates, for the blend PDMS63.

Final steady-state morphology	$\dot{\gamma}$ (s^{-1})	t_1 (s)	$\dot{\gamma}t_1$	t_2 (s)	$\dot{\gamma}t_2$	t_3 (s)	$\dot{\gamma}t_3$
Phase inversion	10	47	470	160	1600	7600	76 000
	15	32	480	90	1350	4900	73 500
	20	11	220	440	8800	7900	158 000
	30	23	690	100	3000	5500	165 000
Refinement	10	53	530	140	1400	7300	73 000
	15	24	360	116	1700	3200	48 000
	20	35	700	120	2400	3800	76 000
	30	29	870	88	2640	2700	81 000

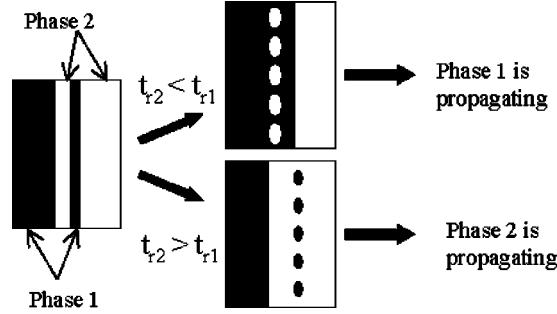


FIG. 9. Schematized mechanisms of breakage of one filament occurring at the boundary of the stripes that leads to the propagation of one phase.

1. Influence of the concentration at a shear rate of 10 s^{-1}

We recorded large discrepancies (up to 20%) in characteristic times between samples at the same concentration. These discrepancies can be explained by the different initial morphologies. The size of the inclusions of HPC50%, and the size and especially the volume of encapsulated droplets of PDMS can be slightly different from one sample to another. The presence and the total volume of encapsulations of PDMS in the sample probably influence the duration of the mechanism of phase inversion. For samples of the same concentration, the phase inversion occurs earlier in blends containing a larger volume of encapsulated PDMS. Considering the experimental variability due to the different initial morphologies and the difficulty of identifying t_1 and t_2 , it is difficult to measure very precisely the influence of concentration on t_1 and t_2 . On the other hand, its influence on t_3 can easily be measured.

The results for t_1 , t_2 , and t_3 are reported in Table III. Only t_3 is plotted in Fig. 6. It is important to observe how, in term of t_3 , concentration has opposite effects on phase inversion and refinement. Below a concentration of 60%, only phase inversion occurs. Increasing the concentration increases the time taken for phase inversion. The time taken follows the reverse trend, decreasing with increasing concentration. At 63%, refinement are sometimes obtained. At 70%, we observe only refinement as the steady-state morphology.

If we fit the two sets of points in Fig. 6 with straight lines, it is interesting to note that the two slopes have similar absolute values. This may indicate that these phenomena are similarly proportional to concentration, in this range of concentration. This makes sense if we recall that both steady-state morphologies are reached through the same mechanism of breaking fiber as schematized in Fig. 9. By making the assumption that the relevant parameter is t_b , the time of breakage of the filament at the boundary of the stripes, t_3 will be the number of filament which must be broken multiplied by the time of breakage of one filament

$$t_3 = n_{\text{HPC50\%}} \cdot t_{b\text{HPC50\%}} < n_{\text{PDMS}} \cdot t_{b\text{PDMS}} \quad \text{in the case of refinement} \quad (9)$$

$$t_3 = n_{\text{PDMS}} \cdot t_{b\text{PDMS}} < n_{\text{HPC50\%}} \cdot t_{b\text{HPC50\%}} \quad \text{in the case of phase inversion,}$$

where $n_{\text{HPC50\%}}$ and n_{PDMS} are, respectively, the average number of filament of HPC50% per stripe of PDMS and the average number of filament of PDMS per stripe of HPC50% and $t_{b\text{HPC50\%}}$ and $t_{b\text{PDMS}}$, respectively, the time of breakage of one filament

of HPC50% and one filament of PDMS. Tsakalos *et al.* (1998) estimated t_b , the time necessary for a drop to break through the development of capillary instabilities in blends of PDMS/HPC50%

$$t_b = \frac{1}{\dot{\gamma}} \cdot \left(\frac{D_0}{d_b(\dot{\gamma})} \right)^2, \quad (10)$$

with

$$d_b \propto \frac{1}{\dot{\gamma}}, \quad (11)$$

where D_0 is the initial diameter of the drop before shearing and $d_b(\dot{\gamma})$ the thread diameter necessary for capillary instabilities leading to breakup. By supposing that

$$\begin{aligned} n_{\text{HPC50\%}} &\propto (1 - \Phi_{\text{PDMS}}) \\ n_{\text{PDMS}} &\propto \Phi_{\text{PDMS}} \end{aligned} \quad (12)$$

and that d_b is independent of concentration [Tsakalos *et al.* (1998)]:

$$\begin{aligned} t_3 &\propto (1 - \Phi_{\text{PDMS}}) \cdot A(\dot{\gamma}) \quad \text{in the case of refinement} \\ t_3 &\propto \Phi_{\text{PDMS}} \cdot B(\dot{\gamma}) \quad \text{in the case of phase inversion,} \end{aligned} \quad (13)$$

where $A(\dot{\gamma})$ and $B(\dot{\gamma})$ are the terms describing dependence on the shear rate. At a given shear rate, the time to obtain a given phase as the continuous phase should be proportional to the concentration of this phase. This is what we observe in Fig. 6.

2. Influence of the shear rate

PDMS63 blends were sheared at various shear rates above 10 s^{-1} , i.e., 15, 20, and 30 s^{-1} . As shown in Table I, the viscosity ratio is the same at these shear rates, but not the elasticity ratio. Increasing the shear rate decreases $G'_{\text{HPC50\%}}/G'_{\text{PDMS}}$ by a factor 2 at 30 s^{-1} (compared to $G'_{\text{HPC50\%}}/G'_{\text{PDMS}} = 1$ at 10 s^{-1}).

Figure 7 shows that the amount of deformation necessary to reach equilibrium is an apparently nonmonotonically function of the shear rate. Deformation versus shear rate for refinement and phase inversion both increase with shear rate, but not at the same rate. Once more, we see here that since the same mechanisms are responsible for both morphologies, external parameters have the same influence on both morphologies. The question remains whether to consider the plateau of deformation between 10 and 20 s^{-1} for refinement and between 20 and 30 s^{-1} for phase inversion as real, or as being simply due to the difficulty of measuring when the steady state is really reached. The only relevant parameters acting in the process are breakup and coalescence, which are monotonically dependent on the shear rate. In addition, the viscosity ratio is constant and the elasticity ratio varies monotonically between 10 and 30 s^{-1} .

If we consider the breakage of filament as the relevant process, it is found from Eqs. (10) and (11) that t_b is proportional to $\dot{\gamma}$. Also, at a given concentration, the deformation for having one phase to be the continuous one should be

$$\text{deformation} = \dot{\gamma} \cdot t_3 \begin{cases} \propto \dot{\gamma}^2 \cdot C(1 - \Phi_{\text{PDMS}}) & \text{in the case of refinement} \\ \propto \dot{\gamma}^2 \cdot D(\Phi_{\text{PDMS}}) & \text{in the case of phase inversion} \end{cases}, \quad (14)$$

where $C(1 - \Phi_{\text{PDMS}})$ and $D(\Phi_{\text{PDMS}})$ regroup terms dependent on concentration. At a given concentration of 63 vol %, this is not what we observe experimentally (Fig. 7). This

demonstrates the limits of this simplified model. The equations for the time necessary for a drop to break [Eq. (10)] and the critical diameter of the filament for breakup [Eq. (11)] proposed by Tsakalos *et al.* (1998) have been established for isolated droplets and so do not take into account the influence of neighboring threads nor the influence of coalescence. Nevertheless, for highly concentrated blends, the surrounding drops and threads probably have an effect on the stability of the filaments. Furthermore, elasticity of the components has not been considered. But the decrease of $G'_{\text{HPC50\%}}/G'_{\text{PDMS}}$ with increasing shear rate certainly influences d_b and t_b . Another question is which D_0 to consider in Eq. (10), especially in the case of $t_{b\text{PDMS}}$ where PDMS is the continuous phase at rest.

IV. CONCLUSIONS

By varying the shear rate applied to blends of PDMS/HPC50%, a flow-induced phase inversion can be observed and studied with rheo-optical microscopy. These observations show that phase inversion occurs after the blend passes through several different transient morphologies. A bifibrillar network structure appears during the transient flow as proposed by Luciani *et al.* (1993). But the subsequent transient stripe morphologies that follow the formation of sheets of PDMS demonstrate that the mechanisms leading to the inverted morphology are more complex. The blends must be subjected to larger deformations (strain units above 70 000) than it was previously reported in a blend where the phase to disperse is the minor and least viscous component [Lazo and Scott (1999)]. In our system, the phase to disperse is the major and most viscous component. Fixing concentration and viscosity ratio, the amount of deformation necessary to reach the phase inversion is not constant and seems to depend on shear rate. This suggests that one of the controlling parameters is the amount of deformation needed to break a filament which is known to be shear rate dependent. At a fixed shear rate of 10 s^{-1} , we did not observe a single clear concentration above which phase inversion would not occur. On the contrary, we rather observed a range of concentration for which either phase inversion or refinement occurs. Again, if the rupture of the filament mechanism is important, its dependence on the elasticity of the matrix and the filament must be taken into account.

References

- Avgeropoulos, G. N., F. C. Weissert, P. H. Biddison, and G. G. A. Böhm, "Heterogeneous blends of polymers. Rheology and morphology," *Rubber Chem. Technol.* **49**, 93–104 (1976).
- Bouilloux, A., B. Ernst, A. Lobbrecht, and R. Muller, "Rheological and morphological study of the phase inversion in reactive polymer blends," *Polymer* **38**, 4775–4783 (1997).
- Bourry, D. and B. D. Favis, "Co-continuity and phase inversion in HDPE/PS blends: influence of interfacial modification and elasticity," *J. Polym. Sci., Part B: Polym. Phys.* **36**, 1889–1899 (1998).
- Chapoy, L. L., "The applicability of a percolation model to photoconductivity in guest-host thermotropic nematic liquid crystal systems," *Chem. Phys.* **84**, 1530–1532 (1986).
- Chappelear, D. C., "Interfacial tension between polymers," *Polym. Prepr. (Am. Chem. Soc. Div. Polym. Chem.)* **5**, 363–371 (1964).
- Favis, B. D. and J. P. Chalifoux, "Influence of composition on the morphology of polypropylene/polycarbonate blends," *Polymer* **29**, 1761–1767 (1988).
- Ghodgaonkar, P. G. and U. Sundararaj, "Prediction of dispersed phase drop diameter in polymer blends: the effect of elasticity," *Polym. Eng. Sci.* **36**, 1656–1665 (1996).
- Guido, S. and N. Grizzuti, "Phase separation effects in the rheology of aqueous solutions of hydroxypropyl-cellulose," *Rheol. Acta* **34**, 137–146 (1995).
- Krieger, I. M. and T. J. Dougherty, "A mechanism for non-Newtonian flow in suspensions of rigid spheres," *Trans. Soc. Rheol.* **3**, 137–152 (1959).
- Lazo, N. D. B. and C. E. Scott, "Morphology development during phase inversion of a PS/PE blend in isothermal, steady-shear flow," *Polymer* **40**, 5469–5478 (1999).

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- Vucnerqu. X0 R0P c x c t f . c p f G0 R g w t g n F l u f l g t . ÷F g h q t o c v k p c p f d t g e n w r o g e j c p k u o u q h u k p i n g f t q r u f w l p i u j g c t . 00 I0 T j g q r 042. 362563638 (3; ; 1)0
- Witcenk N0 C0 ÷Qp v j g x k u e q u k { / e q p e g p t c v k p f g r g p f g p e g q h l o o k u e k d n g r q n o g t d n g p f u . 00 I0 T j g q r 035. 383763859 (3; ; 3)0
- Y k n g o u g . T0 E0 C0 R q u j w o c f g D q g t . I0 x c p F c o . c p f C0 F0 I q u k u . ÷E q / e q p v p w q u o q t r j q n i l g u l p r q n o g t d n g p f u < c p g y o q f g n 00 R q n o g t 39. 7: 9; 67: : 9 (3; ; 1)0
- Y k n g o u g . T0 E0 C0 R q u j w o c f g D q g t . I0 x c p F c o . c p f C0 F0 I q u k u . ÷E q / e q p v p w q u o q t r j q n i l g u l p r q n o g t d n g p f u < v j g l p h n g p e q h v j g l p v g t h e c k n v g p u k p . 00 R q n o g t 40. : 496: 56 (3; ; c)0
- Y k n g o u g . T0 E0 G0 I0 L0 T c o c n g t . I0 x c p F c o . c p f C0 R q u j w o c f g D q g t . ÷O q t r j q n i { f g x g n r o g p v l p l o o k u e k d n g r q n o g t d n g p f u < l p k l e n d n g p f o q t r j q n i { c p f r j c u g f l o g p u k p u . 00 R q n o g t 40. 88736887; (3; ; d)0